

Multi-target DPA attacks: Pushing DPA beyond the limits of a desktop computer

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MOTIVATION

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Question:

- ▶ Can we find **practical** ways to exploit as much of the leakage as possible?

Adversary selects:

T 1x set of trace acquisitions captured over time

F A selected target function (e.g for AES: SubBytes, AddRndKey, MixColumns). The choice of target allows the adversary to make predictions about the value of a **subkey** (e.g first SubBytes operation leaks on first byte of the key)

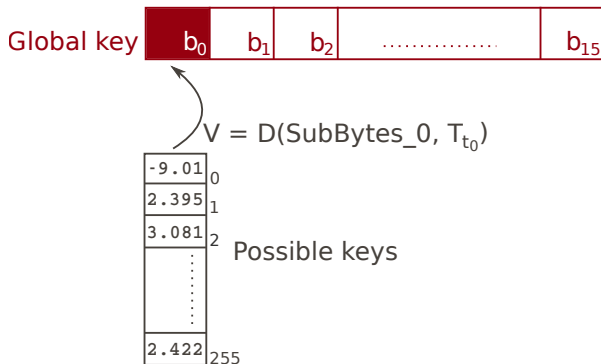
t 1x time point within the set of traces

D A “distinguisher”—statistical tool for guessing subkey values

The attack $D(F, T_t)$ produces a “distinguishing vector” V .

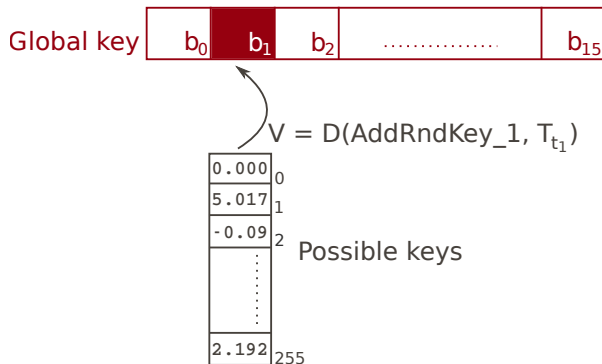
DISTINGUISHING VECTORS

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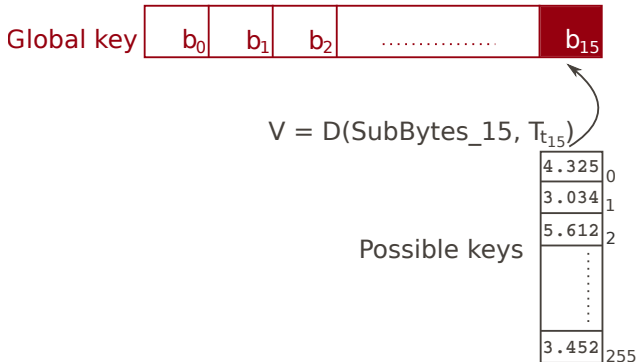
$$V = D(\text{SubBytes}_2, T_{t_2})$$

Possible keys

2.805	0
-1.24	1
0.081	2
⋮	
1.141	255

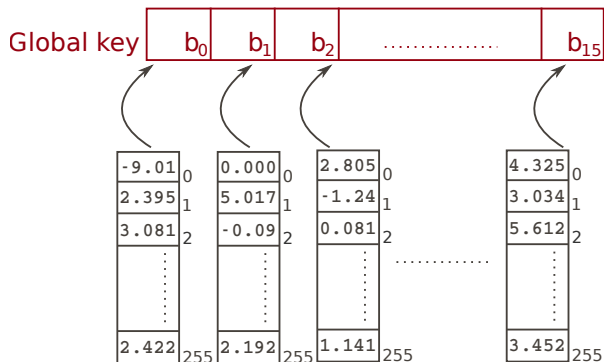
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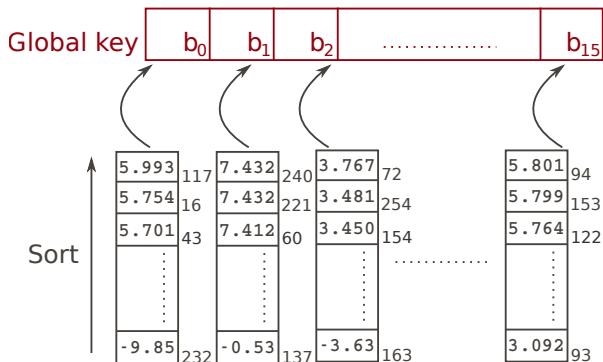
KEY ENUMERATION

- ▶ Correct sub-key value not necessarily ranked first in each distinguishing vector
- ▶ Use key enumeration (Veyrat-Charvillion SAC '12) to search the candidate space



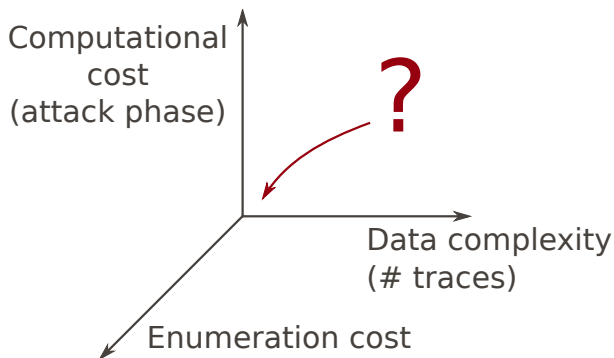
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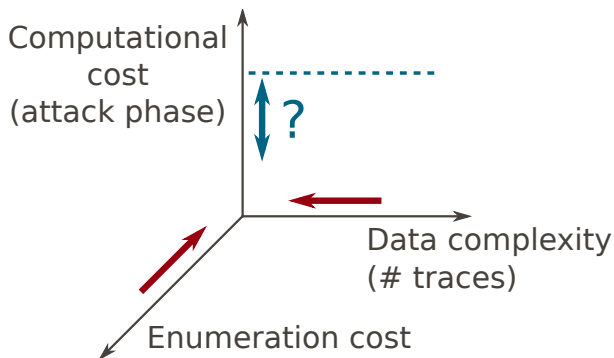
OPTIMALITY

Traditionally optimise for data complexity. But what is the best adversary?

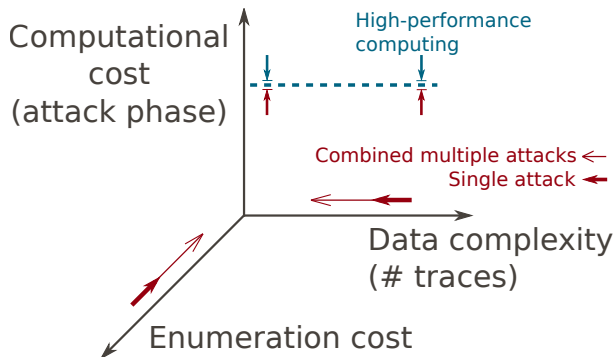


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THIS WORK



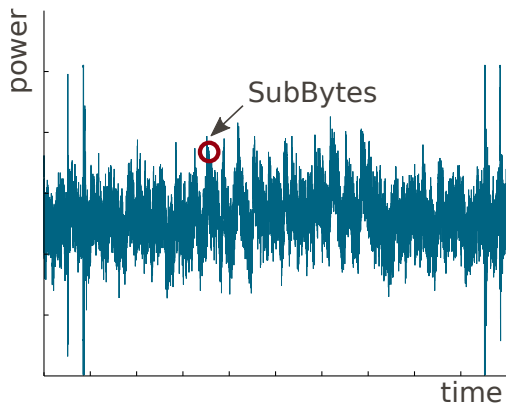
- Idea: improve by running **multiple** DPA attacks and **combining** the key information

MULTIPLE SOURCES OF INFORMATION LEAKAGE

Scenario: find the first key byte of an AES key.

Traditional approach: take results of **single best attack**

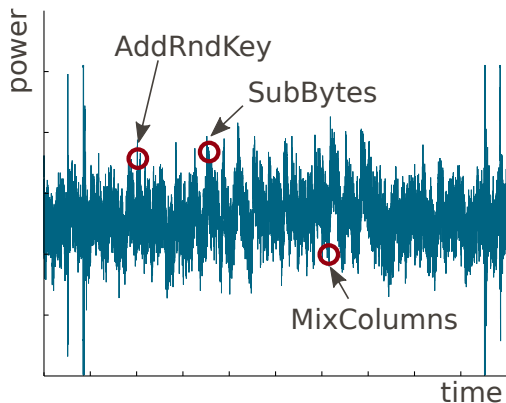
► $V = D(F, T_t)$



MULTIPLE SOURCES OF INFORMATION LEAKAGE

...or combine results calculated using different **target functions**, using best distinguishers and time points?

- ▶ $V = \text{Combine}(D(\mathbf{F}_1, T_{t_1}), D(\mathbf{F}_2, T_{t_2}), \dots)$



METHODOLOGY

Need a method for combining results (distinguishing vectors) of multiple attacks:

- ▶ Ideally: have “probabilities” for subkey candidates
- ▶ Distinguishers don’t (usually) do this—need a conversion method
- ▶ Need to preserve the **ranks** and the **relative distance** between the subkey candidates

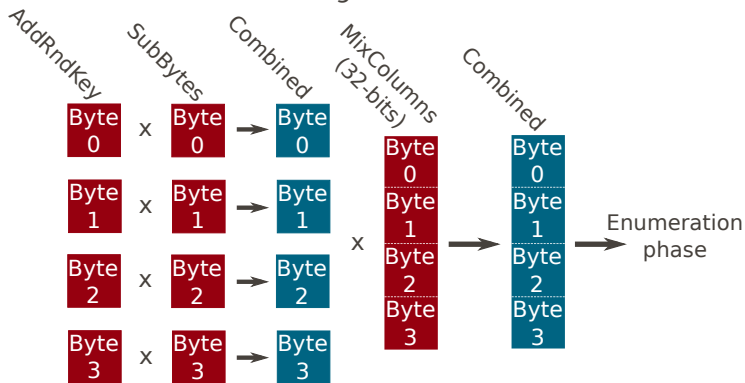
Solution:

Given two distinguishing vectors:

1. Transform to be positive-valued with a baseline of zero
2. Normalise the vector scores to sum to 1
3. Combine vectors by **pointwise multiplying**

AES CASE STUDY

Suppose exploitable information leakage on key bytes 0,...,3 occurs under the 8-bit AddRndKey and SubBytes operations and a 32-bit MixColumns target



Many other combinations possible!

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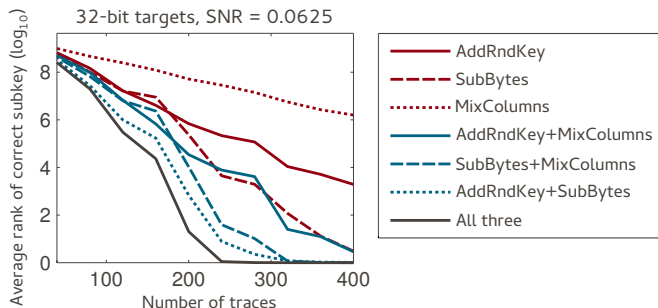
- ▶ **Aim:** compare the best single-target attack against various multiple-target attacks
- ▶ **How:** compare the sizes of the sets of remaining subkey candidates to test after the attacks
- ▶ **Q:** 32-bit targets are time-consuming attacks—can we mitigate this?
- ▶ **Q:** In reality we don't know where leakage occurs—does the combining strategy remain effective here?

SIMULATED EXPERIMENTS

Simulated leakage:

- ▶ Different signal-to-noise ratios
- ▶ Used correlation distinguisher with Hamming weight model

Example results:

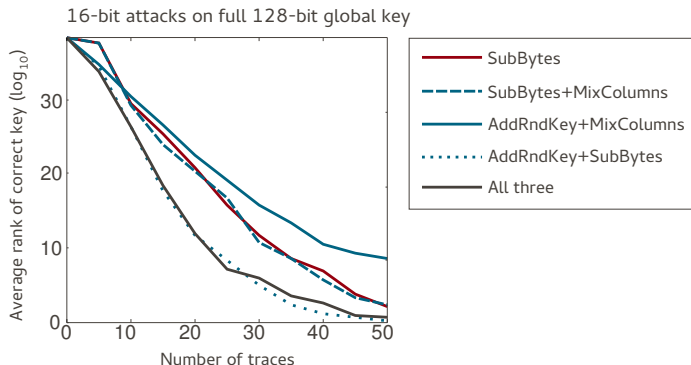


Generally: multi-target attacks did a better job

ARM7 EXPERIMENTS

- ▶ **Strongest adversary:** assume the points at which leakage occurs are known
- ▶ Unprotected AES: 10,000 traces, 200 repeat experiments

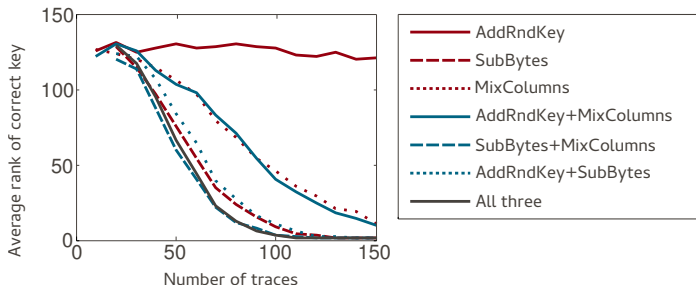
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ARM7 EXPERIMENTS

- ▶ **Weaker adversary:** assume windows of points in which leakage occurs are known
- ▶ Exhaustive search of all combinations of points in the windows

Example results:



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COMPUTATIONAL COST

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- ▶ Need to start accounting for this level of acceleration!

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- ▶ Do enhanced strategies for when we don't know where the leakage is exist?
- ▶ Further exploration into attacks utilising combination as a building block

CONCLUSION

Thanks for listening!